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THE INCREASING ROTATION PERIOD OF COMET 10P/TEMPEL 2

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ABSTRACT

We imaged comet 10P/Tempel 2 on 32 nights from 1999 April through 2000 March. R-band light curves were obtained on 11 of these nights from 1999 April through 1999 June, prior to both the onset of significant coma activity and perihelion. Phasing of the data yields a double-peaked light curve and indicates a nucleus rotational period of 8.941 ± 0.002 hr with a peak-to-peak amplitude of ~ 0.75 mag. Our data are sufficient to rule out all other possible double-peaked solutions as well as the single- and triple-peaked solutions. This rotation period agrees with one of five possible solutions found in post-perihelion data from 1994 by Mueller and Ferrin (Icarus, 123, 463–477) and unambiguously eliminates their remaining four solutions. We applied our same techniques to published light curves from 1988 which were obtained at an equivalent orbital position and viewing geometry as in 1999. We found a rotation period of 8.932 ± 0.001 hr in 1988, consistent with the findings of previous authors and incompatible with our 1999 solution. This reveals that Tempel 2 spun-down by ~ 32 s between 1988 and 1999 (two intervening perihelion passages). If the spin-down is due to a systematic torque, then the rotation period prior to perihelion during the 2010 apparition is expected to be an additional 32 s longer than in 1999.

Key words: comets: general – comets: individual (10P/Tempel2) – methods: data analysis – techniques: photometric

Online-only material: color figure, machine readable and VO tables

1. INTRODUCTION

Comet 10P/Tempel 2 was discovered by E.W.L. Tempel on 1873 July 4. It was recovered in 1878, but not during the 1883 or 1889 apparitions. It has been observed on every return since 1894 except three (1910, 1935, and 1941) when it was particularly poorly placed for observing (Kronk 2003, 2007, 2009). While telescopic improvements now allow it to be observed at every apparition, the roughly 5.5 year period results in apparitions which alternate between favorable and unfavorable viewing geometries. Consequently, Tempel 2 was well placed for observing in 1978, 1988, and 1999, but poorly placed in 1983, 1994, and 2004 when it reached perihelion on the far side of the Sun.

Tempel 2 was extensively observed during its favorable 1988 return. Because it is only weakly active until shortly before perihelion (Sekanina 1979, and references therein) a nucleus light curve can be measured. This allowed a number of investigators to measure the rotation period. The earliest results came from Jewitt & Meech (1988) who found likely periods of 8.9 ± 0.1 hr or 7.5 ± 0.1 hr. Jewitt & Luu (1989) extended these observations to near perihelion, concluding that the rotation period was 8.95 ± 0.01 hr. Comparable periods were determined by A'Hearn et al. (1989) (8.9 hr) and Wisniewski (1990) (8.93 hr). Sekanina (1991) combined these data to determine a sidereal period of 8.93200 ± 0.00006 hr.

Mueller & Ferrin (1996) observed Tempel 2 for three nights 7–9 months after perihelion in 1994, after coma activity had subsided. Their rotation coverage was insufficient to determine a unique period solution, and they found five possible periods due to aliasing: 8.877 hr, 8.908 hr, 8.939 hr, 8.971 hr, and 9.002 hr. All of these periods were incompatible with the 1988 data, and they concluded that "the period is definitely different between the 1988 and the 1994 apparitions." Because of aliasing, it was

not known if Tempel 2 had spun-up or spun-down since 1988, merely that its rotation period had changed.

The idea of comet rotation periods changing due to outgassing dates to Whipple (1950) and his icy conglomerate model of the nucleus, with various authors since then arguing for spin-up or spin-down (see Samarasinha et al. 2004 for a thorough review). Numerical modeling has shown that, depending on the initial conditions, either spin-up or spin-down is possible, with sustained outgassing over many orbits leading to spin-up and ultimately nucleus splitting (Samarasinha & Belton 1995; Neishtadt et al. 2002; Gutiérrez et al. 2003). Measurement of a change in the rotation period of a comet, combined with detailed knowledge of the spin axis orientation, nucleus size and shape, and the outgassing rate can constrain the bulk density and internal structure. Due to the difficulty of studying comet nuclei directly, these properties are only well known for a handful of comets, mostly the result of spacecraft visits.

While simulations have shown that changes in rotation period should be common, a strong case can be made for a changing rotation period in only a few comets: 10P/Tempel 2 (sign of the change unknown prior to this work; Mueller & Ferrin 1996), 2P/Encke (spin-up; Fernández et al. 2005), 9P/Tempel 1 (spin-up; Belton & Drahus 2007; Chesley et al. 2010), and Comet Levy (1990c = C/1990 K1; spin-up; Schleicher et al. 1991; Feldman et al. 1992). The paucity of clear detections of this phenomenon is probably due to the difficulty of obtaining high-quality data sets of the same comet over multiple apparitions. By combining our extensive data obtained during the 1999 apparition with those of previous authors from 1987 to 1988 and 1994, this work will show that 10P/Tempel 2 is the first comet known to spin-down.

We observed Tempel 2 from 1999 April until 2000 March, obtaining images in broadband and narrowband optical wavelengths. Observations prior to perihelion (1999 September 8)

 Table 1

 Summary of Tempel 2 Observations and Geometric Parameters in 1999a

UT	UT	Tel.	CCD	r	Δ	α	Δt	Ecl. Long.	Ecl. Long.	Δm_1^{e}	$\Delta m_2^{\rm f}$	σ_{m_R}	Conditions
Date	Range	Diam.		(AU)	(AU)	(°)	(hr) ^b	Earth (°) ^c	Sun (°)d				
Apr 17	7:48-11:55	1.8 m	SITe	2.025	1.275	24.0	0.177	80.1	56.3	-2.84	-0.02	0.02 – 0.04	Thin clouds
Apr 18	7:20-12:11	1.8 m	SITe	2.020	1.262	23.8	0.176	80.3	56.7	-2.81	+0.08	0.02 - 0.06	Thin clouds
Apr 19	6:53-12:10	1.8 m	SITe	2.014	1.248	23.7	0.174	80.5	57.1	-2.77	+0.03	0.03	Photometric
May 26	6:37-11:22	1.8 m	SITe	1.807	0.839	13.9	0.117	81.9	72.2	-1.36	+0.15	0.01	Thin clouds
May 27	7:43-11:30	1.8 m	SITe	1.802	0.831	13.6	0.116	81.8	72.7	-1.33	+0.26	0.01	Thin clouds
Jun 8	7:05-11:14	1.1 m	TI	1.741	0.748	10.7	0.104	80.1	78.4	-0.92		0.02	Photometric
Jun 9	4:45-09:36	1.1 m	TI	1.736	0.743	10.6	0.103	80.0	78.8	-0.90		0.03	Photometric
Jun 10	4:34-11:17	1.1 m	TI	1.731	0.737	10.5	0.102	79.7	79.3	-0.87	-0.02	0.02	Photometric
Jun 11	4:30-09:35	1.1 m	TI	1.726	0.732	10.4	0.102	79.6	79.8	-0.85		0.02	Photometric
Jun 22	7:29-11:08	1.1 m	TI	1.675	0.685	12.4	0.095	77.5	85.4	-0.69	-0.07	0.02 - 0.06	Thin clouds
Jun 23	3:57-11:04	1.1 m	TI	1.671	0.682	12.7	0.095	77.4	85.9	-0.69	-0.07	0.02 - 0.04	Photometric

Notes.

- ^a All parameters were taken at the midpoint of each night's observations, and all images were obtained at Lowell Observatory.
- ^b Light travel time.
- ^c Ecliptic longitude of the Earth as seen from the comet.
- ^d Ecliptic longitude of the Sun as seen from the comet.
- ^e Magnitude necessary to correct from m_R (r, Δ, α) to m_R (1, 1, 0) for the night (in magnitudes).
- f Offset (in magnitudes) necessary to make data on all nights peak at the same magnitude.

were primarily obtained with a broadband *R* filter to measure the nucleus light curve. Once activity began in earnest, observations were primarily obtained with narrowband comet filters (Farnham et al. 2000) to study coma morphology. In this paper, we consider only the pre-perihelion nucleus light curve in order to resolve the ambiguity about the sign of the change in rotation period and to conclusively demonstrate that Tempel 2 has spun-down since 1988. A second paper (Paper 2) is planned and will utilize data obtained during 2010 in concert with data obtained during the active phase of the 1999 apparition to determine the pole orientation and the location of any active areas.

The layout of the paper is as follows. We summarize our observing campaign and data reductions in Section 2. In Section 3, we analyze the data, determine the rotation period, compare it with earlier data sets, and consider the effects of viewing geometry, coma contamination, and the light curve asymmetry. Finally, in Section 4, we discuss the implications of our results and make predictions for the 2010 apparition.

2. OBSERVATIONS AND REDUCTIONS

2.1. Observing Overview

We obtained images of Tempel 2 on a total of 32 nights between 1999 April and 2000 March, with sampling at monthly or shorter intervals. For the study presented here, we use only the data obtained from 1999 April through 1999 June, with the dates and observing circumstances listed in Table 1. Additional pre-perihelion data were obtained on 1999 July 10, July 16, August 4, August 5, and September 2. However, these nights all had poor weather and the data were unusable for the present study. By 1999 October, the observing window was very short and the comet had extensive coma contamination, making a period determination challenging.

The April and May observations were obtained at the Lowell Observatory Perkins 1.8 m telescope with the SITe 2K CCD. On-chip 4×4 binning of the images produced a pixel scale of 0.61 arcsec. The June observations were obtained at the Hall 1.1 m telescope with the TI 800 CCD. On-chip 2×2 binning produced images with a pixel scale of 0.71 arcsec. At various

times during these runs, we used broadband Kron-Cousins *V* and *R* filters and the HB narrowband comet filters (Farnham et al. 2000). However, as planned, only the *R* filter measurements are extensive enough for the light curve analysis discussed here, so we limit this study to those data. Comet images were guided at the comet's rate of motion. The comet showed evidence of a coma throughout the apparition, progressively increasing with time (see Section 2.4).

2.2. Reductions

The data were reduced using standard bias and flat-field techniques. Landolt standard stars (Landolt 1992) were observed to determine the instrumental magnitude and extinction coefficients on 1999 June 8–11. We observed HB narrowband standard stars (Farnham et al. 2000) on all photometric nights and used these stars as a bootstrap to estimate absolute *R*-band calibrations for the photometric nights on which Landolt standard stars were not observed.

Fluxes were extracted by centroiding on the nucleus and integrating inside circular apertures, with the median sky calculated in an annulus centered on the nucleus with inner and outer radii \sim 33 and \sim 40 arcsec, respectively. By extracting fluxes through a series of circular apertures $(3, 6, 9, \dots, 30 \text{ arcsec radius})$, we monitored the light curve for incursion from passing stars which show up in the larger apertures earlier than the smaller apertures. The 6 arcsec radius aperture gave the most coherent light curve and was used for photometric analysis; this was selected to be large enough to include most of the light from the nucleus even when the seeing was poor and the nucleus point-spread function (PSF) was large, while avoiding as much contamination from passing stars as possible. In order to produce usable light curves from non-photometric nights, we applied extinction corrections and the absolute calibrations from photometric nights with the same telescope and instrument configuration. Thus, we applied the absolute calibrations from April 19 to April 17–18 and May 26-27, and the calibrations from June 23 to June 22. The deviation of the brightness from photometric nights helps give an estimate of how much obscuration was affecting the nonphotometric nights. Field stars on each image were monitored on non-photometric nights to adjust the comet's magnitude for

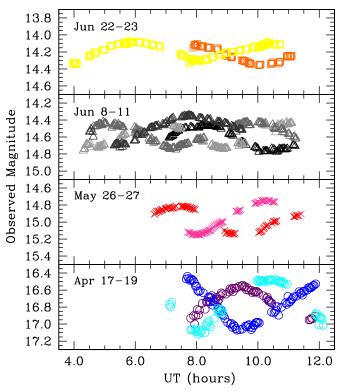


Figure 1. Observed R-band magnitudes (m_R) for our 1999 data plotted as a function of UT on each night. The magnitudes have had absolute calibrations, extinction corrections, and comparison star corrections applied and are given in Column 3 of Table 2. Starting with the bottom panel and moving up, the first panel (circles) displays April 17 (purple), April 18 (blue), and April 19 (cyan). The second panel (crosses) displays May 26 (red) and May 27 (pink). The third panel (triangles) displays June 8 (black), June 9 (light gray), June 10 (medium gray), and June 11 (dark gray). The top panel (squares) displays June 22 (orange) and June 23 (yellow). Note that throughout the time of interest, decreasing r and Δ caused the comet to brighten while at the same time increasing coma damped out the amplitude variations of the nucleus. Thus, the range of magnitudes is different in each panel, although the vertical scale is held constant at 1 mag to emphasize the decreased amplitude.

varying obscuration during the night (discussed in the following subsection).

2.3. Comparison Star Corrections

Relative photometry of the comet with respect to field stars was carried out. However, not enough of the same field stars were available during the entire night and we therefore replaced stars which left the field of view with new ones as they entered. When possible we used only stars brighter than $m_R = 15$, but if fewer than three were available, we used fainter stars, going as faint as $m_R = 16$. Typically between three and six comparison stars were available at a given time.

Reliable catalog magnitudes were not available for enough comparison stars to use comparison stars for absolute calibrations. Therefore, we first used the median of the seven brightest measurements for a given star during the night as its least obscured brightness and determined the adjustment necessary to bring all fainter measurements into agreement. The comparison star correction for an image was the median offset from each star's least obscured brightness during the night for all comparison stars on a given image. Magnitude corrections derived from comparison stars were applied on the nights specified as non-photometric in Table 1. No comparison star corrections were applied for the photometric nights after first using the compar-

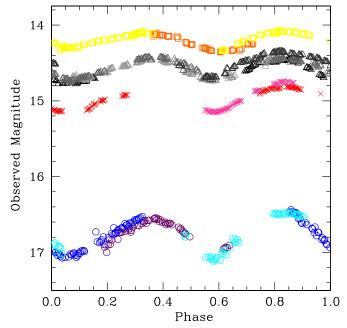


Figure 2. Observed *R*-band magnitudes (m_R) for our 1999 data phased to our best period of 8.941 hr (discussed in Section 3.1). The magnitudes have had absolute calibrations, extinction corrections, and comparison star corrections applied and are given in Column 3 of Table 2. Zero phase was set at perihelion (1999 September 8.424). The points are as given in Figure 1. Note that throughout the time of interest, decreasing r and Δ caused the comet to brighten while at the same time increasing coma damped out the amplitude variations of the nucleus. This figure illustrates the phase coverage obtained during each run and shows that the light curves could be phased even without removing coma contamination.

ison stars to confirm that the nights were indeed photometric. Nightly median comparison star corrections were 0.1–0.4 mag, although some corrections exceeded 1.0 mag on 1999 April 18.

Since the least obscured brightness of the field stars will be fainter than their ideal brightness if it had been photometric, this technique will introduce a systematic nightly magnitude offset from night to night. Therefore, after correcting the relative photometry with field stars, the entire light curve for each night was adjusted so that the peaks for all nights of data were at the same magnitude (Δm_2 , discussed in Section 2.5). If the conditions varied during a night such that there was less obscuration while certain stars were observed but more obscuration while other stars were observed, the uncertainty in the comparison star correction will increase. Hence, the light curves on non-photometric nights may exhibit more scatter.

The calibrated, extinction corrected, and comparison star corrected R magnitudes (m_R) are plotted in Figure 1 as a function of UT. This indicates how much nightly coverage was obtained. In April and May, Tempel 2 was observed for about 5 hr, while in June it was observed for about 7 hr, with the observing window moving earlier each night. Because the comet brightened during the apparition and the coma increased, the median magnitude is different in each figure and later nights have smaller amplitudes (the vertical scale is held fixed in all panels but the range of magnitudes varies from panel to panel). In order to create a uniform data set for period analysis and to study the light curve amplitudes, we removed the coma, corrected for changing r, Δ , and ϕ , and adjusted for nightly offsets. These adjustments will be discussed in the next two sections.

In Figure 2, we show the same data as in Figure 1 but phased to 8.941 hr (our best period which will be discussed in Section 3.1).

This figure emphasizes the increase in brightness and decrease in amplitude throughout the run, as later nights are higher in the figure and have smaller amplitudes. It also demonstrates the phase coverage obtained during each run, making it possible to determine the rotation period even without removing the coma contamination.

2.4. Removal of Coma Contamination

While Tempel 2 is not strongly active, some coma was visible throughout the apparition. The coma contamination is, in general, not large and the rotation period can be determined without coma removal. However, to ensure that it was not affecting our results and to compare the amplitude of the light curve with those obtained by other authors, we removed the coma inside the monitoring aperture. For unchanging grains flowing radially outward from the nucleus at a constant velocity, the coma flux per pixel decreases as ρ^{-1} , where ρ is the projected distance from the nucleus. Since the area of equally spaced annuli increases as ρ , the total coma flux in each annulus should be constant. In reality, the coma often does not fall off as ρ^{-1} and there are factors which may cause further deviation from a constant total flux per annulus such as contamination by background stars or cosmic rays, wings of the nucleus PSF, and imperfect background removal. However, we found that a linear fit to the total annular flux as a function of annular distance from the nucleus (ρ) provides a reasonable first-order approximation of the coma. This is illustrated in Figure 3 using 1999 June 9 as a representative night.

We calculated the total flux in 3 arcsec wide annuli centered on the nucleus (e.g., 0–3 arcsec, 3–6 arcsec, ..., 27–30 arcsec) to create radial profiles (the total annular flux as a function of ρ) for each image. These are plotted as solid light gray curves (images without significant contamination from background stars) and dotted dark gray curves (images with significant contamination from background stars) in Figure 3. We then computed the median total flux in each annulus for the night, ignoring images with obvious contamination from background stars. Next, we fit a straight line to the total annular flux as a function of distance from the nucleus, ρ , (the heavy black line in Figure 3) from $\rho = 7.5$ to 19.5 arcsec for each image (where $\rho =$ 7.5 arcsec was the center of the 6–9 arcsec annulus and $\rho = 19.5$ arcsec was the center of the 18–21 arcsec annulus). This range was chosen to exclude as much of the signal from the nucleus (ρ < 6 arcsec) as possible and to minimize contamination from passing stars ($\rho > 21$ arcsec). We extrapolated the fit in to the nucleus ($\rho = 0$ arcsec) and out to $\rho = 30$ arcsec. The total coma annular flux was removed from the total annular flux to give the coma corrected total annular flux (i.e., the total nucleus annular flux), which was integrated and converted back to magnitudes. Since the monitoring aperture was 6 arcsec in radius, the total coma which was removed for a night was the sum of the total coma annular flux in the 0-3 and 3-6 arcsec radius annuli.

When determining the nightly coma, we excluded images with stars which obviously altered the fit. Stars that contaminate the larger annuli tend to result in an underremoval of coma in the monitoring aperture, while stars closer to the nucleus tend to result in an overremoval of the coma in the monitoring aperture. While we excluded the images with obvious contamination from background stars, fainter stars undoubtedly remain. Since more background stars pass through the larger annuli than the smaller annuli, this results in a systematic underremoval of the coma.

As shown in Figure 3, typical profiles appear to have some curvature. This implies that more coma should be removed than

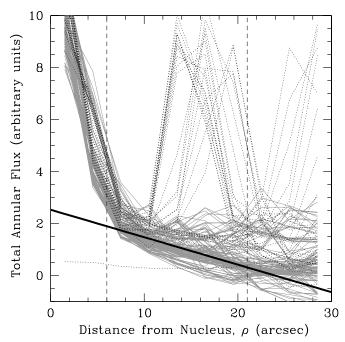


Figure 3. Representative nightly radial profile (1999 June 9). Each curve is composed of the total annular flux (in arbitrary units) in 3 arcsec wide annuli. The solid light gray curves are the radial profiles for images which were used to estimate a nightly median coma profile. The dotted dark gray curves are the radial profiles for images which had contamination by background stars and were not used to determine the nightly median coma profile. The heavy black curve is the nightly median coma profile. This was determined by taking the median of all the light gray curves at the midpoint of each annulus, then fitting a straight line to this nightly radial profile for annuli between 6 and 21 arcsec (the vertical dashed lines), and extrapolating the fit in to the nucleus and out to 30 arcsec. If the coma decreased as ρ^{-1} the coma profile would be a horizontal line. The coma profile was never a horizontal line due to the wings of the nucleus PSF, contamination from background stars, and possibly a non- ρ^{-1} fall off of the coma. We fit a straight line as a first-order approximation. Higher order fits varied more from image to image. See the text for further discussion.

is accomplished with a linear fit. A significant contributor to the curvature at small ρ is likely the wings of the nucleus PSF, while at large ρ , the coma signal may simply be too small and is swamped by uncertainty in the background removal. We considered higher order fits to better match the curvature; a quadratic fit removed 20%–60% more coma while an exponential fit was poor as it often implied negative nucleus counts. Although these fits removed more coma than the linear fit, they varied more from image to image, resulting in wider variance in the estimated coma. Also, small fluctuations in the larger annuli, where there is very little coma, have a large effect on the estimate of the coma contamination for these fits. Therefore, we concluded that a simple linear fit provided the best compromise for approximating the coma profile. We note that if a different fit to the coma were used, it would somewhat alter the amplitude of the light curve but would not change the location of its extrema. Thus, the coma removal technique does not affect the key result of this paper, the period determination (Section 3.1).

To test that our use of a single nightly coma correction was appropriate, we determined linear coma fits for each usable image on a night. We saw no systematic variation in the estimated coma flux within the photometric aperture as a function of rotational phase throughout the entire campaign, confirming that the use of a single nightly median correction was reasonable. As another test of the coma removal technique, we investigated the total annular nucleus flux remaining after

coma removal. The median fraction for all nights of the nucleus flux contained in the 3 arcsec radius aperture relative to the 9 arcsec radius aperture was 85%. The median for the 6 arcsec radius aperture relative to the 9 arcsec radius aperture was 99%. Apertures larger than 9 arcsec in radius were within $\pm 1\%$ of the 9 arcsec radius aperture flux before deviating at $\rho > 21$ arcsec (which was beyond the range of the coma fit). These ratios were relatively constant throughout the apparition. The ratio of the 3 arcsec radius aperture relative to the 9 arcsec radius aperture varied with seeing changes, but the 6 arcsec radius aperture did not change appreciably. This confirms that the 6 arcsec radius aperture is appropriate for photometric monitoring, and that the light lost by not going to larger apertures should be minimal and roughly the same fraction in all images, causing no effect on the amplitude of the light curve, regardless of seeing.

2.5. Magnitude Adjustments

The viewing circumstances changed significantly during our observations. Therefore, we adjusted the nucleus magnitudes using the standard asteroidal normalization

$$m_R(1, 1, 0) = m_{R, cr} - 5\log(r\Delta) - \beta\alpha \tag{1}$$

where $m_R(1, 1, 0)$ is the normalized magnitude at $r = \Delta = 1$ AU and $\alpha = 0^{\circ}$, $m_{R,cr}$ is the apparent magnitude, m_R (which has had the absolute calibrations, extinction corrections, and comparison star corrections applied), with the coma removed, r is the heliocentric distance (in AU), Δ is the geocentric distance (in AU), β is the linear phase coefficient, and α is the phase angle. β is typically 0.03–0.04 mag deg⁻¹ for comets, and we used $\beta = 0.032$ mag deg⁻¹ since it minimized the Δm_2 adjustment (discussed in the following paragraph). Equation (1) removes the secular variation in brightness and allows comparison of all light curves on a similar scale. The geometric corrections are given as Δm_1 in Column 11 in Table 1 at the midpoint of each night's observations.

The geometric corrections do not always bring the light curves from different nights to the same peak brightness, with variations as high as 0.33 mag. This is due to a number of factors, including: bootstrapping Landolt standard stars from HB standards on photometric nights when Landolt stars were not observed; the application of absolute calibrations on non-photometric nights; comparison stars that are normalized to their brightest point in the night rather than a catalog value; and the shape of the coma removed. Therefore, we introduced an additional adjustment, Δm_2 (Column 12 in Table 1), to adjust the individual light curves to a common peak brightness. It should be noted that this factor is introduced to simplify the rotation period analysis and should not be interpreted as representing any particular physical property.

After phasing the data with preliminary Δm_2 values, we refined Δm_2 so that all light curves were aligned at the peak near ~ 0.85 phase when possible. April 17 and June 22 were aligned using the peak near ~ 0.35 phase. Since April 18 and June 9 did not have conclusive peaks, Δm_2 for these nights was estimated based on the cluster of points near phase 0.85.

2.6. Data

The photometry is given in Table 2. Columns 1 and 2 are the UT date and time (at the telescope) at the midpoint of each exposure (adjustments for light travel time are given in Table 1). Column 3 is m_R , the observed R-band magnitude after photometric calibrations, extinction corrections, and comparison star

corrections have been applied. Column 4 is m_R^* , the comaremoved, reduced magnitude $m_R(1,1,0)$ corrected by Δm_2 so that all nights have a similar peak magnitude. We obtained 1016 data points of which 131 were discarded due to contamination from background stars, tracking problems, or cosmic ray hits.

While there are several adjustments which have been applied to arrive at the m_R^* values listed in Table 2, they do not affect the primary focus of the paper: the rotation period determination. The corrections for geometry (Δm_1) and nightly offsets (Δm_2) shift individual nightly light curves up or down, but the locations of the extrema in rotational phase do not change. While the choice of coma removal algorithm affects the amplitude of the light curve, it also leaves the phase of the extrema unchanged. Therefore, the same rotation period could be determined directly from the m_R values prior to the corrections.

Due to the large number of sources of error for each data point (photon uncertainty in comet and background flux, extinction correction, comparison star correction, coma removal), we estimated the effective uncertainty in the magnitude by fitting a smoothed spline through each night's light curve and subtracting the spline fit. The uncertainty for the night was estimated as the standard deviation of the residuals. The uncertainty was not always constant throughout a night since seeing conditions and obscuration varied on the non-photometric nights, so on some nights we estimated the uncertainty for subsections of the light curve. Variations in the comparison star magnitudes were used as an additional indicator of when the uncertainty changed during a night. The range of uncertainties for a night is given in Column 13 in Table 1.

3. MODELING AND INTERPRETATION

3.1. Determining the Rotation Period in 1999

We defined zero phase to be perihelion (1999 September 8.424), and accounted for the light travel time (Column 8 in Table 1) before phasing the data. We used an interactive period search routine within the Data Desk data analysis package⁴ which updates the phased light curves on the fly, allowing us to easily scan through potential periods. We looked for alignment of extrema since they can be identified in phase space even if the magnitudes or amplitudes are different. As the correct solution is approached, the extrema tend to be systematically shifted in phase based on the (color-coded) date of observation, making it easy to quickly hone in on the optimal solution. However, it is difficult to quantitatively estimate the uncertainty in the period since the alignment of the features is probably well away from the optimal solution by the time the eye can distinguish it, therefore overestimating the uncertainty.

We applied this technique to the m_R^* data given in Column 4 of Table 2, finding an observed, i.e., synodic, period of $8.941 \pm 0.002 \,\text{hr}$ for the combined data set (April–June). We examined all period solutions between 4.47 hr (the single-peaked solution) and 13.41 hr (the triple-peaked solution), and 8.941 hr (the double-peaked solution) is the only viable solution between these extremes. The double-peaked shape is expected for a triaxial ellipsoid and was observed by previous authors in 1988 and 1994. We plot the m_R^* data phased to 8.941 hr in the top panel of Figure 4. The bottom panel is phased to 8.932 hr (the period solution from 1988, discussed in the following subsection).

⁴ http://www.datadesk.com

Table 2Table of Photometry

Date ^a	UT ^b	m_R^c	m_R^{*d}	Date ^a	UT ^b	m_R^c	m _R *d	Datea	UT ^b	m_R^c	m_R^{*d}	Datea	UT ^b	m_R^c	m_R*^d
Apr 17	7.848	16.93	14.38	Apr 18	7.980	16.55	13.99	Apr 18	11.623	16.60	14.05	May 26	6.760	14.87	13.95
Apr 17	7.915	16.90	14.34	Apr 18	8.017	16.55	13.99	Apr 18	11.664	16.57	14.01	May 26	6.801	14.88	13.95
Apr 17	7.952	17.00	14.47	Apr 18	8.054	16.61	14.05	Apr 18	11.702	16.57	14.01	May 26	6.838	14.86	13.93
Apr 17	7.989	16.90	14.34	Apr 18	8.091	16.62	14.06	Apr 18	11.739	16.58	14.02	May 26	6.875	14.85	13.92
Apr 17	8.038	16.83	14.25	Apr 18	8.160	16.61	14.05	Apr 18	11.776	16.56	14.01	May 26	6.912	14.85	13.92
Apr 17	8.076	16.89	14.33	Apr 18	8.234	16.63	14.08	Apr 18	11.813	16.55	13.99	May 26	6.992	14.84	13.91
Apr 17	8.112	16.84	14.26	Apr 18	8.395	16.68	14.14	Apr 18	11.851	16.54	13.98	May 26	7.029	14.84	13.91
Apr 17	8.201	16.76	14.16	Apr 18	8.432	16.69	14.15	Apr 18	11.902	16.53	13.96	May 26	7.066	14.84	13.90
Apr 17	8.294	16.83	14.24	Apr 18	8.469	16.74	14.21	Apr 19	7.129	16.77	14.22	May 26	7.103	14.82	13.89
Apr 17	8.331	16.74	14.13	Apr 18	8.506	16.66	14.12	Apr 19	7.170	16.80	14.25	May 26	7.140	14.83	13.90
Apr 17	8.368 8.421	16.73 16.73	14.13 14.13	Apr 18	8.543 8.580	16.78 16.73	14.25 14.20	Apr 19	7.208 7.824	16.74 17.07	14.18 14.57	May 26 May 26	7.191 7.227	14.84 14.83	13.91 13.90
Apr 17 Apr 17	8.458	16.73	14.13	Apr 18 Apr 18	8.621	16.73	14.20	Apr 19 Apr 19	7.889	17.07	14.57	May 26	7.264	14.83	13.90
Apr 17	8.495	16.69	14.07	Apr 18	8.702	16.83	14.31	Apr 19	7.956	17.08	14.59	May 26	7.302	14.83	13.89
Apr 17	8.547	16.72	14.11	Apr 18	8.739	16.81	14.29	Apr 19	7.993	17.06	14.56	May 26	7.339	14.81	13.87
Apr 17	8.637	16.71	14.10	Apr 18	8.777	16.84	14.33	Apr 19	8.031	17.09	14.61	May 26	7.517	14.82	13.88
Apr 17	8.674	16.68	14.07	Apr 18	8.814	16.83	14.32	Apr 19	8.068	17.12	14.64	May 26	7.554	14.82	13.88
Apr 17	8.711	16.73	14.12	Apr 18	8.851	16.89	14.39	Apr 19	8.105	17.07	14.58	May 26	7.591	14.81	13.88
Apr 17	8.748	16.71	14.10	Apr 18	8.888	16.90	14.40	Apr 19	8.142	17.10	14.62	May 26	7.631	14.82	13.88
Apr 17	8.785	16.67	14.04	Apr 18	8.962	16.93	14.44	Apr 19	8.185	17.07	14.59	May 26	7.668	14.82	13.88
Apr 17	8.821	16.63	14.00	Apr 18	9.028	16.98	14.50	Apr 19	8.281	17.10	14.62	May 26	7.705	14.82	13.89
Apr 17	8.893	16.64	14.02	Apr 18	9.109	17.00	14.53	Apr 19	8.319	17.02	14.52	May 26	7.742	14.82	13.88
Apr 17	8.972	16.65	14.02	Apr 18	9.146	16.99	14.52	Apr 19	8.356	16.99	14.48	May 26	7.779	14.84	13.90
Apr 17	9.067	16.62	13.99	Apr 18	9.183	17.04	14.57	Apr 19	8.393	17.02	14.52	May 26	7.819	14.83	13.89
Apr 17	9.104	16.59	13.94	Apr 18	9.220	17.01	14.54	Apr 19	8.430	16.96	14.45	May 26	7.857	14.84	13.91
Apr 17	9.142	16.60	13.96	Apr 18	9.258 9.295	17.03	14.56	Apr 19	8.467	17.03	14.53	May 26	7.894	14.85	13.92
Apr 17	9.179 9.216	16.58 16.61	13.93 13.98	Apr 18	9.293	17.05 17.07	14.59 14.61	Apr 19	8.606 8.692	16.93 16.82	14.41 14.27	May 26	7.931 7.968	14.85 14.85	13.91 13.93
Apr 17 Apr 17	9.210	16.58	13.93	Apr 18 Apr 18	9.332	17.07	14.61	Apr 19 Apr 19	8.730	16.87	14.27	May 26 May 26	8.935	15.10	14.25
Apr 17	9.315	16.58	13.93	Apr 18	9.535	17.06	14.60	Apr 19	8.766	16.82	14.28	May 26	8.974	15.13	14.30
Apr 17	9.421	16.56	13.91	Apr 18	9.611	17.02	14.55	Apr 19	8.804	16.86	14.33	May 26	9.011	15.12	14.28
Apr 17	9.486	16.55	13.91	Apr 18	9.649	17.03	14.56	Apr 19	8.841	16.83	14.29	May 26	9.048	15.12	14.29
Apr 17	9.523	16.54	13.90	Apr 18	9.686	17.01	14.54	Apr 19	8.878	16.87	14.34	May 26	9.085	15.14	14.31
Apr 17	9.560	16.56	13.92	Apr 18	9.723	17.01	14.53	Apr 19	9.987	16.49	13.89	May 26	9.122	15.13	14.30
Apr 17	9.597	16.56	13.91	Apr 18	9.760	17.04	14.57	Apr 19	10.024	16.50	13.91	May 26	9.163	15.13	14.30
Apr 17	9.634	16.59	13.96	Apr 18	9.797	17.07	14.61	Apr 19	10.062	16.48	13.88	May 26	9.200	15.14	14.31
Apr 17	9.671	16.57	13.93	Apr 18	9.836	17.04	14.58	Apr 19	10.099	16.50	13.90	May 26	9.237	15.14	14.31
Apr 17	9.716	16.60	13.96	Apr 18	9.873	17.01	14.54	Apr 19	10.136	16.49	13.90	May 26	9.274	15.13	14.30
Apr 17	9.807	16.60	13.97	Apr 18	9.910	17.01	14.54	Apr 19	10.172	16.49	13.90	May 26	10.044	15.12	14.29
Apr 17	9.844	16.63	14.00	Apr 18	9.947	16.98	14.51	Apr 19	10.211	16.49	13.90	May 26	10.081	15.11	14.27
Apr 17 Apr 17	9.881 9.918	16.62 16.62	13.98 13.99	Apr 18 Apr 18	9.985 10.022	16.98 16.98	14.50 14.50	Apr 19 Apr 19	10.292 10.329	16.51 16.48	13.91 13.89	May 26 May 26	10.119 10.156	15.11 15.10	14.26 14.26
Apr 17	9.955	16.62	13.99	Apr 18	10.022	16.99	14.51	Apr 19	10.366	16.48	13.88	May 26	10.195	15.10	14.23
Apr 17	9.992	16.62	13.99	Apr 18	10.391	16.73	14.20	Apr 19	10.384	16.48	13.88	May 26	10.232	15.07	14.21
Apr 17	10.037	16.64	14.01	Apr 18	10.460	16.86	14.35	Apr 19	10.441	16.48	13.88	May 26	10.269	15.05	14.18
Apr 17	10.219	16.67	14.05	Apr 18	10.541	16.87	14.37	Apr 19	10.478	16.49	13.89	May 26	10.307	15.04	14.18
Apr 17	10.288	16.70	14.09	Apr 18	10.579	16.85	14.35	Apr 19	10.578	16.48	13.88	May 26	10.344	15.03	14.17
Apr 17	10.325	16.68	14.07	Apr 18	10.616	16.83	14.32	Apr 19	10.658	16.49	13.90	May 26	10.484	15.01	14.13
Apr 17	10.362	16.71	14.11	Apr 18	10.653	16.80	14.28	Apr 19	10.696	16.50	13.91	May 26	10.521	14.99	14.11
Apr 17	10.399	16.73	14.13	Apr 18	10.690	16.90	14.40	Apr 19	10.732	16.51	13.92	May 26	10.558	15.00	14.11
Apr 17	10.436	16.75	14.14	Apr 18	10.811	16.80	14.29	Apr 19	10.769	16.51	13.92	May 26	10.596	15.00	14.11
Apr 17	10.473	16.75	14.16	Apr 18	10.917	16.75	14.22	Apr 19	10.806	16.50	13.91	May 26	10.632	14.98	14.10
Apr 17	10.604	16.79	14.21	Apr 18	10.959	16.77	14.24	Apr 19	10.844	16.51	13.92	May 26	11.187	14.94	14.04
Apr 17	11.689	16.95	14.41	Apr 18	10.996	16.67	14.13	Apr 19	10.907	16.53	13.94	May 26	11.225	14.94	14.04
Apr 17	11.726	16.95	14.41	Apr 18	11.033	16.74	14.22	Apr 19	10.974	16.53	13.95	May 26	11.262	14.92	14.01
Apr 17	11.763 11.800	16.93 16.94	14.38 14.39	Apr 18 Apr 18	11.070 11.107	16.74 16.71	14.21 14.18	Apr 19	11.889 11.926	16.89 16.87	14.36 14.35	May 26	11.299 11.353	14.92 14.92	14.02 14.02
Apr 17 Apr 17	11.800	16.94	14.39	Apr 18 Apr 18	11.107	16.71	14.18 14.16	Apr 19 Apr 19	11.926	16.87	14.35	May 26 May 27	7.732	15.12	14.02
Apr 18	7.681	16.47	13.89	Apr 18	11.144	16.68	14.16	Apr 19	12.001	17.01	14.54	May 27	7.777	15.12	14.33
Apr 18	7.718	16.44	13.86	Apr 18	11.277	16.67	14.13	Apr 19	12.038	16.92	14.44	May 27	7.820	15.12	14.34
Apr 18	7.755	16.46	13.89	Apr 18	11.356	16.62	14.07	Apr 19	12.076	16.92	14.44	May 27	7.859	15.15	14.36
Apr 18	7.792	16.48	13.91	Apr 18	11.393	16.64	14.09	Apr 19	12.113	16.95	14.47	May 27	7.899	15.14	14.36
Apr 18	7.829	16.48	13.90	Apr 18	11.431	16.64	14.09	Apr 19	12.151	17.01	14.55	May 27	7.936	15.14	14.35
Apr 18	7.867	16.47	13.90	Apr 18	11.468	16.66	14.12	May 26	6.640	14.91	13.99	May 27	7.974	15.15	14.36
Apr 18	7.906	16.49	13.91	Apr 18	11.505	16.61	14.06	May 26	6.679	14.89	13.97	May 27	8.012	15.15	14.36
Apr 18	7.943	16.51	13.94	Apr 18	11.542	16.61	14.06	May 26	6.716	14.88	13.95	May 27	8.050	15.14	14.36

Table 2 (Continued)

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Date ^a	UT ^b	m_R^c	m_R*^d	Datea	UT ^b	m_R^c	m _R *d	Date ^a	UTb	m_R^c	m_R^{*d}	Date ^a	UT ^b	m_R^c	m_R*^d
May 27	8.088	15.15	14.36	Jun 8	8.275	14.47	13.88	Jun 9	4.817	14.73	14.30	Jun 9	8.848	14.73	14.31
May 27	8.129	15.15	14.37	Jun 8	8.312	14.47	13.89	Jun 9	4.844	14.71	14.26	Jun 9	8.875	14.74	14.31
May 27	8.168	15.14	14.35	Jun 8	8.347	14.46	13.87	Jun 9	4.871	14.71	14.27	Jun 9	8.902	14.74	14.32
May 27	8.206	15.13	14.34	Jun 8	8.382	14.47	13.88	Jun 9	4.900	14.71	14.27	Jun 9	8.929	14.73	14.30
May 27	8.243	15.13	14.34	Jun 8	8.418	14.47	13.89	Jun 9	4.926	14.70	14.26	Jun 9	8.956	14.73	14.30
May 27	8.280	15.13	14.34	Jun 8	8.453	14.47	13.89	Jun 9	4.953	14.70	14.25	Jun 9	8.983	14.73	14.30
May 27	8.317	15.12	14.32	Jun 8	8.490	14.46	13.88	Jun 9	4.980	14.69	14.23	Jun 9	9.010	14.73	14.30
May 27	8.356	15.12	14.32	Jun 8	8.525	14.46	13.87	Jun 9	5.007	14.69	14.24	Jun 9	9.346	14.68	14.22
May 27	8.394	15.10	14.30	Jun 8	8.560	14.47	13.88	Jun 9	5.452	14.64	14.16	Jun 9	9.373	14.67	14.22
May 27	8.431	15.10 15.10	14.30	Jun 8	8.596	14.47	13.89	Jun 9	5.479	14.63	14.15	Jun 9	9.400	14.71	14.27
May 27 May 27	8.468 8.505	15.10	14.30 14.28	Jun 8 Jun 8	8.631 8.676	14.48 14.48	13.90 13.91	Jun 9 Jun 9	5.506 5.533	14.63 14.62	14.15 14.14	Jun 9 Jun 9	9.427 9.454	14.66 14.66	14.21 14.20
May 27	8.544	15.07	14.27	Jun 8	8.711	14.49	13.91	Jun 9	5.560	14.59	14.14	Jun 9 Jun 9	9.434	14.69	14.25
May 27	8.581	15.06	14.25	Jun 8	8.746	14.48	13.90	Jun 9	5.587	14.59	14.09	Jun 9	9.507	14.69	14.25
May 27	8.618	15.04	14.23	Jun 8	8.781	14.49	13.91	Jun 9	5.614	14.58	14.08	Jun 9	9.534	14.69	14.25
May 27	8.655	15.03	14.22	Jun 8	8.816	14.50	13.93	Jun 9	5.641	14.58	14.07	Jun 9	9.561	14.68	14.22
May 27	8.692	15.03	14.21	Jun 8	9.065	14.57	14.02	Jun 9	5.668	14.57	14.06	Jun 9	9.588	14.67	14.21
May 27	8.734	15.02	14.20	Jun 8	9.100	14.56	14.01	Jun 9	5.694	14.57	14.06	Jun 9	10.269	14.47	13.93
May 27	8.771	15.01	14.19	Jun 8	9.135	14.57	14.03	Jun 9	5.986	14.56	14.04	Jun 9	10.561	14.51	13.98
May 27	8.808	15.01	14.18	Jun 8	9.170	14.57	14.02	Jun 9	6.012	14.55	14.03	Jun 9	10.588	14.55	14.03
May 27	8.846	15.00	14.18	Jun 8	9.205	14.59	14.05	Jun 9	6.039	14.54	14.03	Jun 9	10.615	14.49	13.96
May 27	8.883	15.00	14.18	Jun 8	9.489	14.66	14.15	Jun 9	6.066	14.54	14.02	Jun 9	10.642	14.48	13.94
May 27	9.303	14.87	14.02	Jun 8	9.525	14.66	14.15	Jun 9	6.093	14.54	14.03	Jun 9	10.669	14.45	13.90
May 27	9.340	14.88	14.03	Jun 8	9.560	14.67	14.16	Jun 9	6.120	14.55	14.03	Jun 9	10.699	14.47	13.93
May 27	9.377	14.87	14.02	Jun 8	9.595	14.67	14.17	Jun 9	6.147	14.52	14.00	Jun 9	10.726	14.47	13.93
May 27 May 27	9.414 9.451	14.87 14.86	14.02 14.00	Jun 8 Jun 8	9.630 9.908	14.70 14.72	14.21 14.25	Jun 9 Jun 9	6.174 6.201	14.52 14.54	14.00 14.02	Jun 9 Jun 9	10.753 10.780	14.46 14.46	13.91 13.91
May 27	9.431	14.78	13.91	Jun 8	9.908	14.72	14.23	Jun 9 Jun 9	6.457	14.50	13.97	Jun 9 Jun 9	10.780	14.44	13.89
May 27	9.952	14.78	13.91	Jun 8	9.943	14.72	14.24	Jun 9	6.484	14.50	13.96	Jun 9 Jun 9	10.867	14.47	13.92
May 27	9.989	14.77	13.90	Jun 8	10.013	14.74	14.27	Jun 9	6.511	14.49	13.96	Jun 9	10.925	14.44	13.89
May 27	10.026	14.77	13.90	Jun 8	10.048	14.78	14.33	Jun 9	6.538	14.49	13.95	Jun 9	10.952	14.42	13.87
May 27	10.063	14.77	13.91	Jun 8	10.194	14.76	14.31	Jun 9	6.565	14.49	13.95	Jun 9	10.978	14.45	13.91
May 27	10.137	14.75	13.88	Jun 8	10.229	14.77	14.32	Jun 9	6.592	14.48	13.94	Jun 9	11.005	14.45	13.90
May 27	10.175	14.75	13.88	Jun 8	10.265	14.77	14.31	Jun 9	7.256	14.47	13.92	Jun 9	11.032	14.45	13.90
May 27	10.212	14.75	13.88	Jun 8	10.300	14.77	14.31	Jun 9	7.283	14.47	13.92	Jun 9	11.066	14.43	13.88
May 27	10.249	14.74	13.87	Jun 8	10.335	14.77	14.32	Jun 9	7.310	14.48	13.94	Jun 9	11.093	14.43	13.88
May 27	10.291	14.75	13.88	Jun 8	10.467	14.74	14.27	Jun 9	7.337	14.49	13.94	Jun 9	11.120	14.44	13.89
May 27	10.366	14.75	13.88	Jun 8	10.502	14.76	14.30	Jun 9	7.364	14.49	13.95	Jun 10	4.648	14.48	13.93
May 27	10.402	14.75	13.88	Jun 8	10.538	14.74	14.28	Jun 9	7.391	14.50	13.96	Jun 10	4.708	14.48	13.93
May 27 May 27	10.489 10.526	14.76 14.77	13.89 13.90	Jun 8 Jun 8	10.573 10.608	14.76 14.78	14.30 14.33	Jun 9 Jun 9	7.418 7.444	14.49 14.51	13.96 13.97	Jun 10 Jun 10	4.735 4.762	14.47 14.47	13.92 13.92
May 27	10.563	14.76	13.90	Jun 8	10.646	14.77	14.33	Jun 9	7.471	14.49	13.96	Jun 10 Jun 10	4.796	14.47	13.92
May 27	11.425	14.91	14.07	Jun 8	10.681	14.76	14.31	Jun 9	7.498	14.49	13.96	Jun 10	4.829	14.44	13.88
Jun 8	7.113	14.61	14.08	Jun 8	10.716	14.74	14.27	Jun 9	8.011	14.62	14.14	Jun 10	4.856	14.44	13.88
Jun 8	7.148	14.60	14.07	Jun 8	10.751	14.74	14.28	Jun 9	8.038	14.63	14.15	Jun 10	4.882	14.45	13.90
Jun 8	7.184	14.59	14.06	Jun 8	10.786	14.74	14.28	Jun 9	8.065	14.63	14.15	Jun 10	4.909	14.45	13.90
Jun 8	7.219	14.59	14.05	Jun 8	10.837	14.74	14.27	Jun 9	8.092	14.62	14.14	Jun 10	4.936	14.46	13.91
Jun 8	7.254	14.58	14.04	Jun 8	10.872	14.74	14.27	Jun 9	8.119	14.63	14.15	Jun 10	4.963	14.42	13.85
Jun 8	7.293	14.56	14.01	Jun 8	10.907	14.75	14.29	Jun 9	8.146	14.63	14.15	Jun 10	4.990	14.44	13.88
Jun 8	7.328	14.55	13.99	Jun 8	10.942	14.74	14.28	Jun 9	8.173	14.64	14.16	Jun 10	5.017	14.44	13.87
Jun 8	7.363	14.53	13.98	Jun 8	10.977	14.74	14.27	Jun 9	8.199	14.66	14.19	Jun 10	5.044	14.44	13.87
Jun 8	7.398	14.52	13.96	Jun 8	11.160	14.70	14.21	Jun 9	8.226	14.65	14.17	Jun 10	5.070	14.45	13.89
Jun 8	7.434	14.53	13.96	Jun 8	11.195	14.69	14.21	Jun 9	8.253	14.66	14.19	Jun 10	5.249	14.49	13.95
Jun 8	7.568	14.50	13.93	Jun 8	11.230	14.71	14.23	Jun 9	8.494	14.70	14.25	Jun 10	5.276	14.47	13.92
Jun 8 Jun 8	7.643 7.680	14.49 14.49	13.92 13.92	Jun 9	4.315 4.342	14.76 14.74	14.35 14.32	Jun 9	8.521 8.548	14.69 14.72	14.24 14.28	Jun 10 Jun 10	5.303 5.329	14.45 14.47	13.90 13.92
Jun 8	7.814	14.49	13.92	Jun 9 Jun 9	4.342	14.74	14.32	Jun 9 Jun 9	8.575	14.72	14.27	Jun 10 Jun 10	5.356	14.44	13.88
Jun 8	7.814	14.48	13.90	Jun 9 Jun 9	4.308	14.74	14.31	Jun 9 Jun 9	8.602	14.71	14.27	Jun 10 Jun 10	5.383	14.44	13.90
Jun 8	7.890	14.49	13.90	Jun 9	4.422	14.68	14.22	Jun 9	8.629	14.71	14.27	Jun 10 Jun 10	5.410	14.48	13.93
Jun 8	8.024	14.49	13.91	Jun 9	4.451	14.69	14.23	Jun 9	8.656	14.72	14.28	Jun 10	5.437	14.47	13.92
Jun 8	8.060	14.49	13.91	Jun 9	4.478	14.69	14.24	Jun 9	8.682	14.72	14.28	Jun 10	5.464	14.45	13.89
Jun 8	8.095	14.49	13.92	Jun 9	4.505	14.69	14.23	Jun 9	8.709	14.72	14.29	Jun 10	5.491	14.46	13.91
Jun 8	8.134	14.48	13.89	Jun 9	4.531	14.67	14.20	Jun 9	8.736	14.72	14.29	Jun 10	5.519	14.47	13.91
Jun 8	8.169	14.47	13.89	Jun 9	4.558	14.72	14.29	Jun 9	8.768	14.74	14.31	Jun 10	5.573	14.48	13.93
Jun 8	8.204	14.47	13.88	Jun 9	4.764	14.71	14.27	Jun 9	8.795	14.74	14.31	Jun 10	5.600	14.48	13.94
Jun 8	8.239	14.47	13.89	Jun 9	4.790	14.72	14.28	Jun 9	8.822	14.72	14.29	Jun 10	5.627	14.49	13.94

Table 2 (Continued)

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Date ^a	UT ^b	m_R^c	m_R*^d	Date ^a	UT ^b	m_R^c	m_R*^d	Date ^a	UT ^b	m_R^c	m_R^{*d}	Date ^a	UT ^b	m_R^c	m_R*^d
Jun 10	5.990	14.48	13.94	Jun 10	9.560	14.43	13.87	Jun 11	6.487	14.50	14.08	Jun 11	9.503	14.52	14.11
Jun 10	6.017	14.52	13.99	Jun 10	9.586	14.43	13.86	Jun 11	6.514	14.50	14.08	Jun 22	7.910	14.15	13.97
Jun 10	6.043	14.50	13.96	Jun 10	9.613	14.43	13.87	Jun 11	6.541	14.49	14.06	Jun 22	7.942	14.12	13.91
Jun 10	6.070	14.51	13.98	Jun 10	9.640	14.43	13.86	Jun 11	6.568	14.49	14.07	Jun 22	7.971	14.11	13.91
Jun 10	6.097	14.52	13.99	Jun 10	9.667	14.42	13.86	Jun 11	6.594	14.49	14.07	Jun 22	7.998	14.13	13.93
Jun 10	6.124	14.54	14.02	Jun 10	9.694	14.44	13.88	Jun 11	6.657	14.47	14.04	Jun 22	8.027	14.11	13.89
Jun 10	6.151	14.55	14.03	Jun 10	9.721	14.47	13.92	Jun 11	6.684	14.47	14.04	Jun 22	8.085	14.13	13.93
Jun 10	6.178	14.56	14.05	Jun 10	9.748	14.46	13.91	Jun 11	6.711	14.47	14.04	Jun 22	8.143	14.13	13.93
Jun 10 Jun 10	6.204 6.231	14.54 14.53	14.02 14.01	Jun 10 Jun 10	9.775 10.024	14.46 14.43	13.91 13.86	Jun 11 Jun 11	6.737 6.764	14.48 14.46	14.06 14.03	Jun 22 Jun 22	8.173 8.200	14.14 14.14	13.95 13.95
Jun 10 Jun 10	6.460	14.62	14.01	Jun 10 Jun 10	10.024	14.43	13.87	Jun 11	6.906	14.45	14.03	Jun 22	8.227	14.14	13.93
Jun 10	6.487	14.65	14.18	Jun 10	10.031	14.43	13.86	Jun 11	6.933	14.45	14.02	Jun 22	8.368	14.15	13.96
Jun 10	6.513	14.64	14.16	Jun 10	10.105	14.43	13.88	Jun 11	6.960	14.46	14.03	Jun 22	8.394	14.16	13.97
Jun 10	6.540	14.61	14.12	Jun 10	10.132	14.43	13.87	Jun 11	6.986	14.44	14.00	Jun 22	8.421	14.15	13.96
Jun 10	6.567	14.63	14.14	Jun 10	10.159	14.45	13.90	Jun 11	7.013	14.44	13.99	Jun 22	8.669	14.16	13.97
Jun 10	6.594	14.65	14.18	Jun 10	10.185	14.44	13.89	Jun 11	7.076	14.42	13.97	Jun 22	8.695	14.16	13.98
Jun 10	6.621	14.67	14.20	Jun 10	10.212	14.45	13.90	Jun 11	7.138	14.41	13.95	Jun 22	8.722	14.18	14.01
Jun 10	6.648	14.65	14.18	Jun 10	10.239	14.44	13.89	Jun 11	7.165	14.40	13.94	Jun 22	8.946	14.23	14.10
Jun 10	6.674	14.66	14.19	Jun 10	10.266	14.43	13.87	Jun 11	7.192	14.39	13.93	Jun 22	8.973	14.23	14.11
Jun 10	6.701	14.65	14.18	Jun 10	10.496	14.45	13.90	Jun 11	7.219	14.38	13.91	Jun 22	9.000	14.25	14.13
Jun 10	6.921	14.71	14.26	Jun 10	10.523	14.49	13.95	Jun 11	7.246	14.37	13.90	Jun 22	9.124	14.25	14.14
Jun 10 Jun 10	6.948 6.974	14.71 14.71	14.26 14.26	Jun 10 Jun 10	10.550 10.577	14.50 14.51	13.97 13.98	Jun 11 Jun 11	7.515 7.541	14.37 14.37	13.90 13.90	Jun 22 Jun 22	9.151 9.178	14.27 14.26	14.17 14.15
Jun 10 Jun 10	7.001	14.71	14.28	Jun 10 Jun 10	10.577	14.49	13.95	Jun 11	7.568	14.36	13.88	Jun 22	9.178	14.20	14.13
Jun 10 Jun 10	7.001	14.71	14.27	Jun 10	10.769	14.51	13.98	Jun 11	7.595	14.37	13.89	Jun 22	9.516	14.30	14.23
Jun 10	7.055	14.71	14.27	Jun 10	10.796	14.51	13.98	Jun 11	7.622	14.35	13.87	Jun 22	9.543	14.30	14.24
Jun 10	7.082	14.72	14.28	Jun 10	10.823	14.54	14.02	Jun 11	7.651	14.36	13.88	Jun 22	9.570	14.31	14.25
Jun 10	7.109	14.74	14.31	Jun 10	10.850	14.52	13.99	Jun 11	7.678	14.36	13.88	Jun 22	9.597	14.31	14.25
Jun 10	7.136	14.74	14.31	Jun 10	10.877	14.55	14.03	Jun 11	7.705	14.35	13.87	Jun 22	9.650	14.31	14.26
Jun 10	7.162	14.74	14.32	Jun 10	11.001	14.57	14.06	Jun 11	7.732	14.35	13.87	Jun 22	9.707	14.33	14.29
Jun 10	7.231	14.73	14.29	Jun 10	11.028	14.56	14.05	Jun 11	7.759	14.34	13.86	Jun 22	9.734	14.34	14.31
Jun 10	7.258	14.73	14.30	Jun 10	11.055	14.59	14.09	Jun 11	7.788	14.35	13.86	Jun 22	9.761	14.33	14.30
Jun 10	7.285	14.73	14.29	Jun 10	11.180	14.60	14.11	Jun 11	7.815	14.35	13.87	Jun 22	9.788	14.34	14.31
Jun 10	7.339	14.75	14.33	Jun 10	11.207	14.60	14.10	Jun 11	7.842	14.35	13.87	Jun 22	10.047	14.36	14.34
Jun 10	7.366 7.392	14.73 14.72	14.29 14.28	Jun 10	11.234 11.263	14.62	14.14	Jun 11	7.869 7.896	14.36 14.36	13.88 13.89	Jun 22 Jun 22	10.074 10.101	14.35	14.33 14.32
Jun 10 Jun 10	7.392 7.446	14.72	14.26	Jun 10 Jun 11	4.516	14.62 14.54	14.13 14.14	Jun 11 Jun 11	8.093	14.38	13.89	Jun 22 Jun 22	10.101	14.35 14.34	14.32
Jun 10	7.473	14.70	14.25	Jun 11	4.544	14.53	14.13	Jun 11	8.120	14.38	13.91	Jun 22	10.461	14.33	14.30
Jun 10	7.505	14.69	14.24	Jun 11	4.573	14.50	14.09	Jun 11	8.147	14.38	13.90	Jun 22	10.488	14.32	14.27
Jun 10	7.532	14.70	14.24	Jun 11	4.616	14.54	14.14	Jun 11	8.174	14.39	13.92	Jun 22	10.687	14.34	14.31
Jun 10	7.559	14.70	14.25	Jun 11	4.644	14.60	14.23	Jun 11	8.201	14.39	13.92	Jun 22	10.714	14.32	14.27
Jun 10	7.586	14.70	14.24	Jun 11	5.322	14.70	14.39	Jun 11	8.355	14.39	13.92	Jun 22	10.741	14.31	14.26
Jun 10	7.613	14.68	14.22	Jun 11	5.349	14.69	14.38	Jun 11	8.382	14.39	13.93	Jun 22	10.949	14.26	14.15
Jun 10	7.640	14.68	14.23	Jun 11	5.376	14.68	14.36	Jun 11	8.409	14.40	13.94	Jun 22	10.976	14.25	14.14
Jun 10	7.667	14.69	14.23	Jun 11	5.403	14.68	14.36	Jun 11	8.436	14.40	13.94	Jun 22	11.002	14.25	14.13
Jun 10	7.693	14.68	14.22	Jun 11	5.429	14.68	14.37	Jun 11	8.463	14.39	13.92	Jun 22	11.059	14.25	14.15
Jun 10 Jun 10	7.720 7.747	14.67 14.68	14.21 14.21	Jun 11 Jun 11	5.459 5.486	14.68 14.69	14.36 14.38	Jun 11	8.689 8.716	14.42 14.42	13.96 13.97	Jun 22 Jun 22	11.086 11.113	14.26 14.24	14.15 14.13
Jun 10 Jun 10	8.012	14.64	14.21	Jun 11 Jun 11	5.513	14.73	14.38	Jun 11 Jun 11	8.743	14.42	13.97	Jun 22 Jun 23	3.963	14.24	14.13
Jun 10	8.039	14.64	14.16	Jun 11	5.540	14.69	14.38	Jun 11	8.770	14.42	13.97	Jun 23	3.999	14.34	14.36
Jun 10	8.066	14.63	14.14	Jun 11	5.567	14.67	14.35	Jun 11	8.797	14.43	13.98	Jun 23	4.026	14.33	14.33
Jun 10	8.092	14.64	14.16	Jun 11	5.596	14.72	14.42	Jun 11	8.920	14.43	13.99	Jun 23	4.052	14.34	14.35
Jun 10	8.119	14.63	14.14	Jun 11	5.623	14.69	14.37	Jun 11	8.947	14.43	13.99	Jun 23	4.079	14.33	14.33
Jun 10	8.146	14.62	14.13	Jun 11	5.650	14.69	14.37	Jun 11	8.974	14.44	14.01	Jun 23	4.106	14.35	14.37
Jun 10	8.227	14.61	14.12	Jun 11	5.677	14.69	14.37	Jun 11	9.001	14.45	14.01	Jun 23	4.492	14.26	14.19
Jun 10	8.254	14.61	14.12	Jun 11	5.704	14.69	14.38	Jun 11	9.028	14.45	14.01	Jun 23	4.519	14.24	14.17
Jun 10	9.289	14.46	13.91	Jun 11	5.976	14.65	14.31	Jun 11	9.158	14.47	14.04	Jun 23	4.546	14.24	14.17
Jun 10	9.315	14.47	13.92	Jun 11	6.003	14.64	14.30	Jun 11	9.184	14.48	14.06	Jun 23	4.606	14.23	14.15
Jun 10	9.342	14.45	13.90	Jun 11	6.030	14.64	14.29	Jun 11	9.211	14.48	14.06	Jun 23	4.676	14.21	14.11
Jun 10	9.369	14.45	13.90	Jun 11	6.057	14.57	14.19	Jun 11	9.238	14.48	14.06	Jun 23	4.703	14.21	14.11
Jun 10 Jun 10	9.396 9.423	14.46 14.45	13.91 13.89	Jun 11 Jun 11	6.084 6.215	14.58 14.58	14.20 14.20	Jun 11 Jun 11	9.265 9.329	14.49 14.54	14.07 14.14	Jun 23 Jun 23	4.730 4.963	14.20 14.17	14.10 14.04
Jun 10 Jun 10	9.423	14.45	13.89	Jun 11 Jun 11	6.242	14.57	14.20	Jun 11 Jun 11	9.329	14.54	14.14	Jun 23 Jun 23	4.903	14.17	14.04
Jun 10	9.477	14.46	13.91	Jun 11	6.269	14.55	14.16	Jun 11	9.423	14.50	14.09	Jun 23	5.017	14.17	14.05
Jun 10	9.503	14.44	13.88	Jun 11	6.296	14.55	14.15	Jun 11	9.449	14.51	14.11	Jun 23	5.202	14.12	13.95
Jun 10	9.533	14.43	13.88	Jun 11	6.323	14.55	14.15	Jun 11	9.476	14.52	14.11	Jun 23	5.229	14.14	13.97

Table 2 (Continued)

Date ^a	UT ^b	m_R^c	m_R^{*d}	Date ^a	UT ^b	m_R^c	m_R^{*d}	Date ^a	UT ^b	m_R^c	m_R*^d	Date ^a	UT ^b	m_R^c	m_R*^d
Jun 23	5.256	14.13	13.97	Jun 23	6.617	14.12	13.94	Jun 23	8.151	14.31	14.30	Jun 23	9.922	14.15	14.00
Jun 23	5.444	14.11	13.93	Jun 23	6.773	14.13	13.96	Jun 23	8.315	14.28	14.24	Jun 23	10.021	14.15	14.00
Jun 23	5.471	14.11	13.92	Jun 23	6.800	14.14	13.98	Jun 23	8.342	14.29	14.26	Jun 23	10.048	14.14	13.99
Jun 23	5.498	14.10	13.92	Jun 23	6.827	14.14	13.99	Jun 23	8.368	14.30	14.27	Jun 23	10.075	14.15	14.00
Jun 23	5.628	14.09	13.90	Jun 23	7.473	14.22	14.12	Jun 23	8.496	14.26	14.20	Jun 23	10.103	14.13	13.97
Jun 23	5.655	14.10	13.90	Jun 23	7.500	14.23	14.15	Jun 23	8.523	14.26	14.21	Jun 23	10.130	14.13	13.97
Jun 23	5.682	14.11	13.92	Jun 23	7.527	14.23	14.15	Jun 23	8.549	14.26	14.21	Jun 23	10.157	14.11	13.94
Jun 23	5.710	14.11	13.92	Jun 23	7.557	14.24	14.17	Jun 23	8.761	14.24	14.16	Jun 23	10.186	14.11	13.93
Jun 23	5.737	14.11	13.93	Jun 23	7.584	14.24	14.16	Jun 23	8.788	14.23	14.14	Jun 23	10.213	14.12	13.95
Jun 23	5.764	14.10	13.92	Jun 23	7.611	14.24	14.17	Jun 23	8.815	14.24	14.16	Jun 23	10.240	14.12	13.94
Jun 23	5.808	14.08	13.88	Jun 23	7.759	14.34	14.35	Jun 23	8.944	14.21	14.11	Jun 23	10.269	14.12	13.95
Jun 23	5.834	14.07	13.87	Jun 23	7.786	14.32	14.32	Jun 23	8.971	14.21	14.11	Jun 23	10.296	14.09	13.90
Jun 23	5.861	14.08	13.89	Jun 23	7.812	14.28	14.24	Jun 23	8.998	14.20	14.10	Jun 23	10.323	14.09	13.90
Jun 23	5.894	14.07	13.87	Jun 23	7.843	14.28	14.24	Jun 23	9.149	14.20	14.08	Jun 23	10.357	14.11	13.92
Jun 23	5.921	14.08	13.88	Jun 23	7.870	14.30	14.27	Jun 23	9.176	14.20	14.10	Jun 23	10.384	14.09	13.89
Jun 23	5.947	14.09	13.89	Jun 23	7.897	14.30	14.28	Jun 23	9.203	14.20	14.09	Jun 23	10.411	14.10	13.91
Jun 23	6.123	14.08	13.88	Jun 23	7.929	14.29	14.26	Jun 23	9.407	14.19	14.07	Jun 23	10.524	14.11	13.92
Jun 23	6.150	14.09	13.90	Jun 23	7.956	14.29	14.26	Jun 23	9.434	14.18	14.05	Jun 23	10.551	14.11	13.92
Jun 23	6.177	14.09	13.89	Jun 23	7.982	14.30	14.28	Jun 23	9.461	14.17	14.04	Jun 23	10.578	14.13	13.96
Jun 23	6.341	14.09	13.89	Jun 23	8.012	14.30	14.29	Jun 23	9.607	14.17	14.03	Jun 23	10.709	14.11	13.92
Jun 23	6.368	14.10	13.91	Jun 23	8.039	14.29	14.27	Jun 23	9.634	14.16	14.02	Jun 23	10.742	14.12	13.94
Jun 23	6.395	14.11	13.93	Jun 23	8.066	14.30	14.27	Jun 23	9.661	14.17	14.03				
Jun 23	6.563	14.11	13.93	Jun 23	8.097	14.30	14.28	Jun 23	9.868	14.14	13.99				
Jun 23	6.590	14.13	13.96	Jun 23	8.124	14.30	14.27	Jun 23	9.895	14.13	13.97				

^a UT date of observations. All data were obtained in 1999.

(This table is also available in machine-readable and Virtual Observatory (VO) forms in the online journal.)

The uncertainty in the period was estimated from the smallest offset that produced light curves that were visibly out of phase. Figure 5 illustrates an exaggeration of this process using three periods: 8.937 hr (top), 8.941 (middle), and 8.945 (bottom). Note that these periods are separated by double the estimated error to emphasize the trend in the location of the extrema. We plot the m_R^* data offset vertically by -0.015 mag day⁻¹ since 1999 April 17 to better show the chronological progression of the light curves. In the top panel, later light curves (higher on the plot) occur at a later phase, while in the bottom panel later light curves occur at an early phase. This clearly illustrates that the correct solution is between the two, making it easy to identify 8.941 hr as the optimal period. The inclusion of the April data is vital for this process, as the larger separation between April and the later data sets decreases the range of possible solutions.

For comparison, we also conducted period searches using Fourier (Deeming 1975) and phase dispersion minimization (PDM; Stellingwerf 1978) techniques. The Fourier routine "Period04" (Lenz & Breger 2005) found a single-peaked period of 4.4705 ± 0.0001 hr. Since we expect the light curve to be double-peaked, this implies a rotation period twice as long, or 8.9409 ± 0.0002 hr (the difference in the last digit is due to rounding). The routine determined an uncertainty in frequency and we converted this to a period uncertainty, although we note that the uncertainty of 0.0002 hr seems unrealistically small. We used our own PDM routine, which found a double-peaked period of 8.941 ± 0.005 hr. We estimated the period uncertainty by finding the range of solutions that had θ (a measure of the

goodness of fit) within 50% of the minimum θ . The agreement between methods confirms the robustness of our period solution.

3.2. Different Rotation Periods Due to Geometry?

The default rotation period obtained by simply phasing the data is the synodic period, the length of time until the brightness appears the same from the Earth. This period changes during the apparition because the illuminated portion of the nucleus seen by the Earth varies as both the Earth and the comet move in their orbits. The sidereal rotation period is the rotation period relative to a fixed position in inertial space. A third period is the solar period, which is the time until the Sun is in the same place in the sky as seen by the comet. Because the synodic and solar rotation periods depend on the orientation of the rotational pole, converting them to a sidereal period requires a pole solution.

Since the synodic period also depends on the position of the Earth, we must consider the geometry of the Earth–comet–Sun system during our observations to confirm that the synodic period changes slowly enough that measuring a single synodic period for the whole 10 week time span is sensible. As seen from the comet, the ecliptic longitude of the Earth (Column 9 of Table 1) and the ecliptic latitudes of the Sun and Earth all changed by less than 5° during our observations, resulting in minimal changes to the measured rotation period. While the ecliptic longitude of the Sun as seen from the comet (Column 10 of Table 1) changed by $\sim\!30^{\circ}$, the net effect on the rotation period was still small due to the likely pole orientation (discussed in the following paragraph), and obtaining a single (synodic) rotation period for the whole time span was valid.

^b UT at midpoint of the exposure (uncorrected for light travel time).

^c Observed R-band magnitude (after applying absolute calibrations, extinction corrections, and comparison star corrections) in a circular aperture with radius 6 arcsec.

^d Coma-removed $m_R(1,1,0)$ corrected by Δm_2 (given in Table 1) so that all nights have the same peak magnitude.

⁵ http://www.univie.ac.at/tops/Period04/

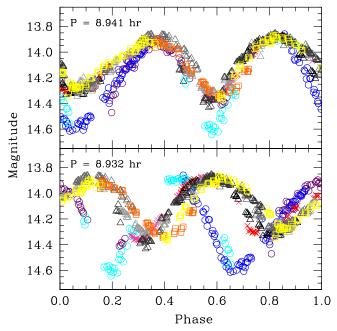


Figure 4. 1999 data phased to the 8.941 hr period (top panel) and the 8.932 hr period (bottom panel). The magnitudes are m_R^* (given in Column 4 of Table 2). The midpoint of each image was used and then corrected for the light travel time, with zero phase set at perihelion (1999 September 8.424). The points are as given in Figure 1.

To confirm this, we investigated the synodic rotation periods which would be observed at different times for pole solutions within 20° in the comet's orbital coordinate system (obliquity and azimuthal angle) of the pole solution given by Sekanina (1987). This range of solutions was chosen to include the pole solution found by Sekanina (1991) for the 1988 apparition and a preliminary pole solution for our 1999 coma morphology data (we will explore this in detail in Paper 2). We considered three runs discretely: April 17-19, May 26-27, and June 22–23 (the June 8–11 run gave similar results to the June 22-23 run), and determined the synodic-sidereal offset which would be observed for all pole solutions under consideration. The difference between the synodic and sidereal periods was 0.000 to +0.003 hr during the April run, 0.000 to +0.002 hr during the May run, and -0.001 to +0.001 hr during the late-June run. Considering the entire 10 week interval as a single large run (i.e., April 17-June 23), the best synodic period differed from the sidereal period by 0.000 to +0.002 hr. Thus, the changing geometry during our observations did not introduce an error in the period determined from the entire run larger than the estimated uncertainty in the synodic period of 0.002 hr (although if the April run was considered by itself, the maximum difference was 0.003 hr). Note that the sign of the synodic-sidereal difference reverses for a pole orientation in the opposite direction, i.e., when the comet has retrograde spin and "north" is defined in the opposite hemisphere.

The above example suggests that changes in the synodic period may be detectable during an apparition. We considered subsets of our 1999 data to look for such a change. There was no discernible difference when the rotation period was determined using all the April and May data or all the May and June data (both intervals gave acceptable solutions from 8.940 to 8.942 hr with a best period of 8.941 hr). We also determined the synodic period between every combination of individual nights from different runs for which a synodic period could be determined. We phased each pair of nights and defined the midpoint between

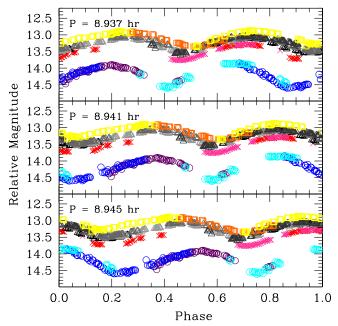


Figure 5. Our 1999 data phased to 8.937 hr (top panel), 8.941 hr (middle panel), and 8.945 hr (bottom panel). The magnitudes are m_R^* (given in Column 4 of Table 2) offset by -0.015 mag per day from 1999 April 17. This offset has been applied for display purposes to minimize overlapping data so the trend in the phasing of extrema is more apparent. The midpoint of each image was used and then corrected for the light travel time before phasing, with zero phase set at perihelion (1999 September 8.424). The symbols are as given in Figure 1. By phasing the data in this manner, we found a best period of 8.941 hr and an uncertainty of ± 0.002 hr.

the two nights as the date corresponding to the measured synodic period. This method suggests an increase in the synodic period of $\sim 0.002\,\mathrm{hr}$ from early-May to mid-June, although the scatter in the individual synodic measurements is very large and the range of acceptable solutions for each pair is generally at least $\pm 0.002\,\mathrm{hr}$. If correct, this requires that the "north" pole be in the opposite hemisphere as was determined by Sekanina (1987), i.e., retrograde rather than prograde rotation.

3.3. Reanalysis of the 1988 Data

We reanalyzed the publicly available data sets from 1988 (Jewitt & Luu 1989; A'Hearn et al. 1989; Wisniewski 1990), defining zero phase at perihelion (1988 September 16.738). The observing scenarios for these data sets are summarized in Table 3. Jewitt & Luu (1989) removed coma from their June data but not the February or April data. A'Hearn et al. (1989) obtained optical and thermal IR data simultaneously on different telescopes and removed coma from the optical data but not from the thermal IR data, which were shown to be nearly free of coma. Wisniewski (1990) did not remove coma from his data. The 1987 data from Jewitt & Meech (1988) were not included in the 1988 period determination because they were too far away in time and were at a much different location in the orbit, making it impossible to directly compare the synodic rotation periods.

We normalized the published magnitudes to $m_R(1,1,0)$ using $\beta = 0.032$ mag deg⁻¹ as was used with our 1999 data. After this normalization, the optical magnitudes still differed by several tenths of a magnitude between runs and authors. We therefore adjusted all the light curves to peak at the same magnitude for the maximum near zero phase by applying nightly Δm_2 values (given in Column 12 of Table 3). We call these data m_R^* and used them for our period search. Δm_2 corrects for nightly differences

Table 3
Table of Photometry

UT Date ^a	Tel. ^b	Instrument	Primary Filter	r (AU)	Δ (AU)	α (°)	Δt (hr) ^c	Ecl. Long. Earth (°) ^d	Ecl. Long. Sun (°) ^e	Δm_1^{f}	$\Delta m_2^{\rm g}$	Ref.h
1987 Mar 31	KP2.1	TI 2	R	3.991	3.162	9.0	0.438	332.6	341.6	-5.79	+0.45	JM
1987 Apr 1	KP2.1	TI 2	R	3.987	3.168	9.2	0.439	332.5	341.7	-5.80	+0.45	JM
1987 Apr 2	KP2.1	TI 2	R	3.984	3.174	9.4	0.440	332.3	341.8	-5.81	+0.45	JM
1987 Apr 3	KP2.1	TI 2	R	3.981	3.181	9.7	0.441	332.2	341.9	-5.82	+0.45	JM
1988 Feb 25	MH2.4	MASCOT	R	2.384	1.985	24.0	0.275	54.3	29.9	-4.14	-0.05	JL
1988 Feb 27	MH2.4	MASCOT	R	2.371	1.949	24.1	0.270	54.9	30.4	-4.09	-0.05	JL
1988 Feb 28	MH2.4	MASCOT	R	2.365	1.932	24.1	0.268	55.1	30.7	-4.07	-0.05	JL
1988 Feb 29	MH2.4	MASCOT	R	2.359	1.914	24.1	0.265	55.4	30.9	-4.04	-0.05	JL
1988 Apr 9	MH1.3	MASCOT	R	2.103	1.279	20.0	0.177	61.7	42.8	-2.79	+0.30	JL
1988 Apr 10	MH1.3	MASCOT	R	2.097	1.265	19.8	0.175	61.7	43.1	-2.75	+0.27	JL
1988 Apr 12	MH1.3	MASCOT	R	2.084	1.239	19.3	0.172	61.8	43.8	-2.68	+0.30	JL
1988 Apr 15	MH1.3	MASCOT	R	2.065	1.201	18.6	0.166	61.8	44.8	-2.57	+0.30	JL
1988 May 8	SO2.3	TI	VR^{i}	1.919	0.959	13.2	0.133	59.3	53.4	-1.75		WI
1988 May 9	SO2.3	TI	VR	1.913	0.951	13.1	0.132	59.1	53.8	-1.72		WI
1988 May 20	ML1.5	Photometer	VR	1.845	0.873	12.8	0.121	56.5	58.3	-1.44	-0.10	WI
1988 May 21	ML1.5	Photometer	VR	1.839	0.867	12.9	0.120	56.2	58.7	-1.43	-0.10	WI
1988 May 22	ML1.5	Photometer	VR	1.832	0.861	13.1	0.119	56.0	59.2	-1.41	-0.10	WI
1988 Jun 10	IRTF	Bolometer	N	1.720	0.788	19.9	0.109	51.3	68.0	-1.30	+11.80	AH
1988 Jun 10	UH2.2	Photometer	6840 Å ^j	1.720	0.788	19.9	0.109	51.3	68.0	-1.30	+0.73	AH
1988 Jun 11	IRTF	Bolometer	N	1.714	0.785	20.4	0.109	51.1	68.4	-1.30	+11.70	AH
1988 Jun 11	UH2.2	Photometer	6840 Å ^j	1.714	0.785	20.4	0.109	51.1	68.4	-1.30	+0.73	AH
1988 Jun 12	ML1.5	Photometer	VR	1.708	0.783	20.9	0.108	50.9	68.9	-1.30	+0.25	WI
1988 Jun 14	ML1.5	Photometer	VR	1.697	0.780	21.9	0.108	50.5	69.9	-1.31	+0.25	WI
1988 Jun 22	MH2.4	BRICC	R	1.653	0.771	25.9	0.107	49.5	74.1	-1.36	+0.23	JL
1988 Jun 23	MH2.4	BRICC	R	1.647	0.770	26.3	0.107	49.4	74.6	-1.36	+0.28	JL
1988 Jun 30	MH2.4	BRICC	R	1.611	0.769	29.7	0.107	49.2	78.4	-1.42	+0.45	JL
1994 Oct 26	KP0.9	T2KA	R	2.498	1.640	14.2	0.227	247.5	234.2	-3.52		MF
1994 Dec 18	KP0.9	T2KA	R	2.802	1.932	11.3	0.268	234.8	245.5	-4.03		MF
1994 Dec 19	KP0.9	T2KA	R	2.807	1.944	11.6	0.269	234.6	245.7	-4.06		MF

Notes.

between data sets due to differences in the extinction correction, absolute calibration, and coma removal (or lack thereof). We do not list a Δm_2 for the A'Hearn et al. (1989) 4845 Å data, as we did not use them when phasing the data since the 4845 Å and 6840 Å data were obtained alternately throughout both nights, and their light curve shapes were nearly identical (although the 6840 Å data were brighter).

Visually scanning the 1988 data for a double-peaked solution, as was done for our 1999 data, yielded a period of $8.932 \pm 0.001\,\mathrm{hr}$. This period agrees with the synodic periods determined for the 1988 data by Sekanina (1991) $(8.931 \pm 0.001\,\mathrm{hr})$, given in his Table 5) and Mueller & Ferrin (1996) (8.933 ± 0.002) .

The viewing geometry in 1988 was nearly identical to the viewing geometry in 1999; the ecliptic latitudes of the Earth and Sun changed minimally and the ecliptic longitudes of the Earth and Sun (given in Columns 9 and 10, respectively, in Table 3) mimicked the changes in 1999. As with the 1999 data (Section 3.1), we considered discrete runs spanning the range of 1988 observations: February 24-28, April 8-12, May 18-22, and June 19-23, and determined the synodic-sidereal difference during each run for the range of pole solutions. Because of the similar viewing geometry, the synodic-sidereal difference was almost the same as in 1999: +0.001 to +0.002 hr for February 24–28, +0.001 to +0.002 hr for April 8–12, 0.000 to +0.001 hr for May 18–22, and -0.001 to +0.001 hr for June 19–23. Considering the entire 1988 time span from February 25 until June 30 as a single large run, the difference in the synodic and sidereal rotation periods was 0.000 to +0.002 hr for the range of pole solutions. As with 1999, the synodic-sidereal difference changes sign for a pole orientation in the opposite direction.

^a Parameters were determined for 7:00 UT on the date of observation.

b Telescope abbreviations: IRTF = NASA Infrared Telescope, KP0.9 = Kitt Peak 0.9 m, MH1.3 = McGraw-Hill 1.3 m, MH2.4 = McGraw-Hill 2.4 m, ML1.5 = Mt. Lemmon 1.5 m, SO2.3 = Steward Observatory 2.3 m, UH2.2 = University of Hawaii 2.2 m.

^c Light travel time.

^d Ecliptic longitude of the Earth as seen from the comet.

^e Ecliptic longitude of the Sun as seen from the comet.

^f $m_R(1, 1, 0)$ correction for the night (in magnitudes).

^g Offset (in magnitudes) necessary to make data on all nights peak at the same magnitude.

h Reference abbreviations: AH = (A'Hearn et al. 1989), JL = (Jewitt & Luu 1989), JM = (Jewitt & Meech 1988), MF = (Mueller & Ferrin 1996), WI = (Wisniewski 1990).

ⁱ The VR filter was centered at 5886 Å with a 2160 Å half-width (Wisniewski 1990).

j A similar number of observations was also made at 4845 Å. However, we primarily used the 6840 Å data and so Δm_2 is only listed for the 6840 Å data. Both of these filters are part of the International Halley Watch filter set (Osborn et al. 1990).

⁶ We did not see evidence of a 13 minute offset of the 1988 April data from Jewitt & Luu (1989) as suggested by Sekanina (1991), but note that Δm_2 could mask this effect. Sekanina (1991) adjusted these data by 13 minutes to derive the quoted synodic period, while Mueller & Ferrin (1996) omitted these data entirely from their period analysis. We include them with no time adjustment.

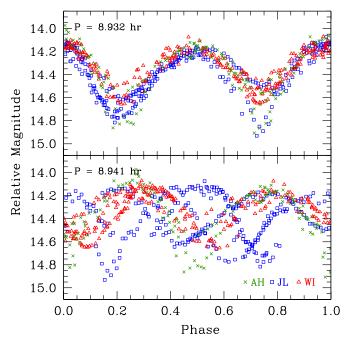


Figure 6. 1988 data from the literature phased to the 8.932 hr period (top panel) and the 8.941 hr (bottom panel). The published data have been normalized to $m_R(1, 1, 0)$ and offset by Δm_2 (given in Table 3) to peak at the same magnitude. The times are as given in the literature and corrected for the light travel time, and zero phase was defined at perihelion (1988 September 16.738). The green crosses (AH) are A'Hearn et al. (1989), the blue squares (JL) are Jewitt & Luu (1989), and the red triangles (WI) are Wisniewski (1990).

(A color version of this figure is available in the online journal.)

Thus, we can directly compare our 1988 solution (8.932 hr) with our 1999 solution (8.941 hr). In Figure 6, we plot the 1988 m_R^* data phased to our period solution from 1988 in the top panel and to our period solution from 1999 in the bottom panel. Similarly, we plot our 1999 m_R^* data phased to 8.941 hr (top panel) and 8.932 hr (bottom panel) in Figure 4. Figures 4 and 6 demonstrate that the rotation periods were clearly different in 1988 and 1999. Since the synodic periods differed by ~ 0.009 hr and synodic–sidereal offsets were similar each apparition, we can conclude that the sidereal periods also differed by ~ 0.009 hr, and thus the rotation period increased from 1988 to 1999.

We looked for a change in the synodic period during the 1988 observations by phasing every combination of pairs of observing runs, e.g., Jewitt & Luu's (1989) February data with A'Hearn's et al. (1989) June data, Jewitt & Luu's (1989) February data with Wisniewski's (1990) June data, etc. Assigning the date of each pair as the midpoint between the two runs, there was no discernible trend in the measured synodic period over time, with acceptable values varying from 8.931 to 8.933 hr with a typical uncertainty of ± 0.001 hr. This is consistent with the conclusions of Jewitt & Luu (1989) who found no change in the rotation period within their uncertainty when analyzing their February, April, and June data as discrete sets. In contrast, Sekanina (1991) found a decrease in the synodic period during the 1988 observations of $\sim 0.003 \, hr$ (his Table 5 and Figure 7). These discrepancies and our possible finding of a slight increase in the rotation period in 1999 (Section 3.1) suggest that Sekanina's (1987) pole solution may not be definitive, with the alternate sense of rotation possible as well (resulting in a "north" pole in the exact opposite position). We will use the coma morphology visible in our post-perihelion 1999 images, combined with data

we will obtain in 2010, to attempt to determine a more robust pole solution in Paper II.

3.4. Reanalysis of the 1994 Data

We also reanalyzed the Mueller & Ferrin (1996) data from 1994, normalizing the published magnitudes to $m_R(1, 1, 0)$ and visually scanning for possible solutions. The data do not yield an unambiguous double-peaked light curve due to undersampling. Mueller & Ferrin (1996) found five possible solutions: 8.877 hr, 8.908 hr, 8.939 hr, 8.971 hr, and 9.002 hr, and we concur with their results. Only one of these, 8.939 hr, is within the uncertainty of our 1999 solution (8.941 \pm 0.002 hr).

Using the same range of pole solutions as in Section 3.2, we find the maximum difference between the synodic and sidereal periods in 1994 October–December was smaller than -0.001 hr (actually about -1 s), in agreement with the difference found by Mueller & Ferrin (1996). Thus, the expected difference between the synodic and sidereal rotation periods is much less than the difference between the five possible solutions. Furthermore, since there were no intervening perihelion passages between the 1994 and 1999 observations, the sidereal rotation period was likely unchanged between these observations. Therefore, we rule out the remaining four possible solutions from Mueller & Ferrin (1996) and conclude that Tempel 2 had spun-down by \sim 0.009 hr (\sim 32 s) between the 1988 and 1994 determinations, which spanned two perihelion passages, and was unchanged between the 1994 post-perihelion observations and our 1999 pre-perihelion observations.

3.5. Coma Contamination and Light Curve Amplitude

Tempel 2 was non-stellar in appearance throughout our 1999 observations. The presence of a coma suppressed the amplitude of the light curve, with the suppression increasing later in the apparition as activity increased. The mean coma removed from the 6 arcsec radius monitoring aperture was 0.20 mag from April 17 to 19, 0.27 mag from May 26 to 27, 0.40 mag from June 8 to 11, and 0.65 mag from June 22 to 23. We measured light curve amplitudes ranging from 0.2 to 0.5 mag prior to removal of the coma. After coma removal, the April 17-19 data exhibited amplitudes of ~ 0.75 mag while all subsequent runs had amplitudes of 0.45–0.50 mag. If a quadratic fit to the coma was used instead of a linear fit, the amplitudes increased to ~ 0.80 in April and 0.50-0.60 in May and June. However, note that as discussed in Section 2.4, we opted for a more conservative linear fit rather than a higher order fit because the higher order fits varied more from image to image and produced less reliable results. Our measured amplitudes in 1999 are similar to the maximum optical amplitudes reported by other authors in 1988 when the comet was at a similar viewing geometry and activity level: 0.65 ± 0.05 mag in February and 0.60 ± 0.05 mag in April (no coma removal; Jewitt & Luu 1989), 0.5 mag in May (no coma removal; Wisniewski 1990), and 0.7 ± 0.1 mag in June (coma removed; Jewitt & Luu 1989).

A'Hearn et al. (1989) measured an amplitude of 0.8 mag in their $10.1 \,\mu\text{m}$ data in 1988 June, exceeding all measured optical amplitudes at similar times in both 1988 and 1999. While the amplitudes measured by ourselves and others approach the thermal IR amplitude, all are somewhat lower, and even a quadratic coma removal from our data cannot bring the amplitudes into agreement. This discrepancy raises two possible interpretations. First, the coma removal techniques employed here and by Jewitt & Luu (1989) and A'Hearn et al. (1989)

are not adequately estimating the coma inside the photometric aperture. To push the amplitude up to $\sim\!0.80,\,50\%\!-\!150\%$ more coma would need to be removed from our May and June data, requiring a significantly steeper curve than even a quadratic fit. Alternatively, the convergence of multiple authors on an optical amplitude of 0.6–0.7 mag in 1988 June and 1999 June may indicate that this is in fact the correct optical amplitude and is different from the thermal IR amplitude. This possibility was suggested by A'Hearn et al. (1989) based on work by Brown (1985) who showed that the amplitude of the thermal IR light curve may be dependent on both wavelength and elongation.

The varying light curve amplitudes will be utilized in Paper 2 when we determine the pole solution using the coma morphology from 1999 and 2010. As the viewing geometry varies during an apparition, the amplitude of the light curve will vary because different cross sections of the nucleus are observed. Thus, the light curve amplitudes will be useful in refining the pole solution and will help in constraining the shape of the nucleus.

We looked for evidence of periodicity in the coma signal by plotting both the total flux and flux per square arcsec in each photometric annulus as a function of rotational phase. What structure is visible on individual nights does not repeat in a coherent manner from night to night or from run to run. There was also no evidence of propagation of any features (either a maximum or minimum signal) outward during a night. This is consistent with the analyses of Jewitt & Luu (1989) and A'Hearn et al. (1989) who did not see a rotation signal in their data.

3.6. Light Curve Asymmetry

The rotational light curve in 1999 is somewhat asymmetric, allowing identification of certain features many rotations apart and eliminating N - 0.5, N + 0.5, N + 1.5, etc. (where N is the number of cycles) as possible solutions. This conclusively rules out the single- and triple-peaked solutions and reduces the uncertainty in the period determination since it halves the number of possible rotations. Any clear description of the light curve shape is made challenging because it is never observed completely on a given night. However, we note the following apparently repeated features: the minimum near 0.6 phase is deeper and steeper than the minimum near 0.1 phase when comparing light curves from the same observing run. There is a shoulder in the rising portion between 0.15 and 0.30 phase. Finally, while there are no nights in which both maxima were clearly observed, the maximum near 0.85 phase may be slightly higher than the maximum near 0.35 phase. We see evidence for each of these features in the 1988 data when discrete observing runs are considered.⁷ The features are also seen in the 1994 data from Mueller & Ferrin (1996), although since the viewing geometry was very different, we cannot be sure that they correspond to the same topographic features on the nucleus.

4. SUMMARY AND DISCUSSION

We imaged Tempel 2 on 32 nights from 1999 April until 2000 March. We present here *R*-band nucleus light curves obtained on

11 of these nights from April through June (prior to perihelion), a total of 892 data points. Absolute calibrations and nightly extinction corrections were determined on photometric nights and were applied to non-photometric nights to extract usable light curves. Field stars in the image were monitored on all nights and were used as comparison stars to correct the comet magnitude on non-photometric nights. A median coma was determined each night and removed from all images on the night. All magnitudes were normalized to $r=\Delta=1\,\mathrm{AU}$ and $\alpha=0^\circ$. A final adjustment, which accounts for uncertainties in the calibrations that tend to create nightly magnitude offsets such as the application of absolute calibrations on non-photometric nights, was applied to make each night peak at the same magnitude.

We determined a synodic rotation period of $8.941 \pm 0.002 \,\mathrm{hr}$; no other double-peaked solutions exist. Our data set is sufficient to rule out all aliases other than the single- and triple-peaked solutions, and these are ruled out by the differences in shape and brightness between the two minima. Our period matches one of the possible periods obtained by Mueller & Ferrin (1996) from post-perihelion data in 1994 (during the same inter-perihelion time as our 1999 data) and rules out their other four possible solutions. We reanalyzed published data from 1988 using the same analysis techniques and found a synodic rotation period of 8.932 ± 0.001 hr. Our 1999 data cannot be fit by the rotation period from 1988, nor can the 1988 data be fit by the rotation period from 1999, even though the comet had nearly identical viewing geometries during the two sets of observations. Thus, we conclude that Tempel 2 spun-down by $0.009 \, \text{hr} (\sim 32 \, \text{s})$ from 1988 to 1999, an interval that included two perihelion passages.

This marks the first conclusive measurement of spin-down in a comet, although three comets have shown possible evidence of spin-up: 9P/Tempel 1 (Belton & Drahus 2007; Chesley et al. 2010), 2P/Encke (Fernández et al. 2005), and Comet Levy (1990c) (Schleicher et al. 1991; Feldman et al. 1992). Modeling by Samarasinha & Belton (1995), Neishtadt et al. (2002), Gutiérrez et al. (2003), and others has shown that either spin-up or spin-down is possible, with spin-up more likely in the long run. These simulations have shown that under certain conditions the spin period can change by much larger amounts in a single orbit (e.g., typical changes of 0.01–10 hr per orbit according to Gutiérrez et al. 2003) than the measured change of 0.009 hr in two orbits for Tempel 2. Thus, the measured spin-down of 10P/Tempel 2 is probably not exceptional, and comparable changes in period could likely be measured in other comets if similarly high-quality data were obtained over several

Possible causes of a change in spin state are summarized by Samarasinha et al. (2004). The spin-down of Tempel 2 may have been caused by either a one-time event or by recurring torquing each orbit. Scenarios for causing a one-time change in rotation period include a short-lived, freshly exposed active region (causing temporary torquing), fragmentation (changing the moment of inertia), collision with another object, and tidal torquing from Jupiter. The orbit of Tempel 2 is well known and tidal torquing from Jupiter should not have been significant or more severe between 1988 and 1999 than on other recent orbits. Collisions are rare in the current solar system, and any collision significant enough to alter the rotation period of Tempel 2 would likely have resulted in an increase in brightness upon subsequent orbits, which has not been seen. Fragmentation is known to be relatively common, occurring on average at least once per century per comet (cf. Chen & Jewitt 1994; Weissman 1980).

⁷ The 1988 April data from Jewitt & Luu (1989) showed the deeper minimum to be at \sim 0.7 phase, in contradiction to all other 1988 data sets (see Figure 6). This data set was the most difficult to normalize since neither April 9 or 12 contained a clear extremum, and the April 10 and 15 data required very different Δm_2 adjustments to bring the maxima in alignment near zero phase. Given that the minima were observed only five nights apart and no light curve change in shape is expected during this short a time interval, we are skeptical of this anomalous minimum.

However, there is no evidence for Tempel 2 having split, such as a companion nucleus or a sustained increase in brightness as was observed in 73P/Schwassmann-Wachmann 3 (Ferrín 2010). A new active region could be created by fragmentation, impact, or outburst. Since outbursts are known to occur far more frequently than fragmentation or impacts, an outburst is the most plausible explanation for a one-time change in the rotation period. If the change in the period was caused by a unique event such as an outburst, it could have occurred anywhere in the orbit and we would expect no change in the rotation period on subsequent orbits.

It is challenging to devise a mechanism that is strong enough to affect the rotation period but lasts for a short time (less than one orbit). Thus, we suspect the spin-down is due to torques on the nucleus caused by asymmetric outgassing. This is believed to be the most common means of changing the spin state of a comet (cf. Samarasinha et al. 2004). Seasonal illumination of an active region could cause torquing which slows the rotation of the nucleus by a comparable amount each orbit. In the case of Tempel 2, the torquing likely occurs near or shortly after perihelion, when the comet is most active, although the length of time over which the torquing may occur is unknown. Since Tempel 2 reached perihelion twice between the 1988 and 1999 observations, in this, our preferred scenario, the rotation period must be changing by ~ 16 s each orbit.

Tempel 2 reached perihelion on 2010 July 4, and we encourage its observation throughout the apparition to determine the rotation period. Due to a perturbation by Jupiter between the 1999 and 2005 apparitions, the viewing geometry is different in 2010 than in 1988 or 1999. The post-perihelion viewing geometry will be better this apparition and the comet will be visible longer each night. The smaller post-perihelion Δ in 2010 will provide better spatial resolution, making it easier to separate the nucleus and coma signals even though the coma is more extensive after perihelion. This may allow measurement of a nucleus light curve after perihelion, despite increased coma contamination relative to the pre-perihelion measurements in 1988, 1994, and 1999.

Assuming the spin-down is recurrent each orbit, we predict that the pre-perihelion rotation period should be \sim 32 s longer than in 1999 as there have been two intervening perihelion passages (1999 September 8 and 2005 February 15) since our data were obtained in 1999. If the pole position given by Sekanina (1987) is correct, the sidereal rotation period should be $8.950 \pm 0.003 \,\mathrm{hr}$. Since it is unknown if the spin-down is caused by an instantaneous impulsive event or a steady change over an extended period of time, we cannot estimate the rotation period that might be observed shortly after perihelion in 2010. Observations long enough after perihelion to allow the torquing to have taken effect should reveal an additional lengthening of the sidereal rotation period by ~ 16 s relative to the pre-perihelion 2010 period. Using again the pole solution of Sekanina (1987), this would yield a sidereal period 8.954 \pm 0.004 hr.

We have begun to observe Tempel 2 in 2010 and will combine these new data with our observations obtained during its active phase in 1999 as a follow-up to the current paper. As of 2010 August (when the revised manuscript was submitted), we are unaware of any period determinations from 2010 observations. In Paper 2, we will use the different viewing geometry provided by the 2010 apparition to investigate the pole orientation and

the location and activity of any jets. We hope to determine the rotation period in 2010, and possibly obtain additional post-perihelion observations after activity has subsided in 2011 or later to resolve whether the comet spins down each orbit. With its relatively low inclination ($i \sim 12^{\circ}$) and perihelion close to Earth's orbit ($q \sim 1.4\,\mathrm{AU}$), Tempel 2 is frequently on the short list of targets for comet missions, making further study highly desirable.

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